

Name: \_\_\_\_\_

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MATH 107

Quiz 5

1) For  $f(x) = \sqrt[3]{x+1}$ ,  $g(x) = 4x^2 - x$  find:

a.  $(g \circ f)(0)$

b.  $(f \circ g)(\frac{1}{2})$

c.  $(f \circ f)(-2)$

2) Use the given pair of functions  $f(x) = 3 - x^2$ ,  $g(x) = \sqrt{x + 1}$  to find and simplify the expression  $(g \circ f)(x)$  and state the domain of each using interval notation.

3) Show that the given function is one-to-one and find its inverse. Check your answers algebraically and graphically.

$$f(x) = \frac{x}{1 - 3x} .$$

4) The price of a media player is given as a function of the weekly sales  $x$  according to the formula  $p(x) = 550 - 30x$  for  $0 \leq x \leq 40$ .

- a. Find  $p^{-1}(x)$  and state its domain.
- b. Find and interpret  $p^{-1}(125)$ .
- c. Find  $x$  if  $p^{-1}(x) = 0$

5) Perform the indicated operations and simplify.

$$\sqrt{x} + \frac{x-1}{\sqrt{x}}$$

6) Find all real solutions for  $2x - 1 = \sqrt{x + 3}$ .

7) Solve the inequality  $12 - \sqrt{x - 3} \leq 15$ .

8) Evaluate the expressions.

a.  $\ln(e^4)$

b.  $\log_6\left(\frac{1}{36}\right)$

c.  $\log_{13}(\sqrt{13})$

d.  $\ln(42^{6\log(1)})$

9) For  $f(x) = e^x$ ,  $g(x) = 10 - e^{-x}$ , sketch the graph of  $y = g(x)$  by starting with the graph of  $y = f(x)$  and using transformations. Track at least three points of your choice and the horizontal asymptote through the transformations. State the domain and range of  $g(x)$ .

10) Earthquakes are complicated events and it is not our intent to provide a complete discussion of the science involved in them. Instead, we refer the interested reader to a solid course in Geology or the U.S. Geological Survey's Earthquake Hazards Program found here and present only a simplified version of the Richter scale. The Richter scale measures the magnitude of an earthquake by comparing the amplitude of the seismic waves of the given earthquake to those of a "magnitude 0 event", which was chosen to be a seismograph reading of 0.001 millimeters recorded on a seismometer 100 kilometers from the earthquake's epicenter. Specifically, the magnitude of an earthquake is given by  $M(x) = \log\left(\frac{x}{1000}\right)$  where  $x$  is the seismograph reading in millimeters of the earthquake recorded 100 kilometers from the epicenter.

- a. Show that  $M(0.001) = 0$ .
- b. Compute  $M(70,000)$ .
- c. If the magnitude of the earthquake was 6.7 on the Richter scale, what was the seismograph reading?